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Reading List

ARCH basics

- Kirchgässner G., J. Wolters (2006 / 2007): Einführung in die moderne Zeitreihenanalyse. München: Vahlen. / Introduction to Modern Time Series Analysis. Berlin: Springer. (Chapter 7)
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Overview of multivariate GARCH

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SV basics

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Realised Volatility

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